

# Number of Neutrino Types

The neutrinos referred to in this section are those of the Standard  $SU(2) \times U(1)$  Electroweak Model possibly extended to allow nonzero neutrino masses. Light neutrinos are those with  $m < m_Z/2$ . The limits are on the number of neutrino mass eigenstates, including  $\nu_1$ ,  $\nu_2$ , and  $\nu_3$ .

## THE NUMBER OF LIGHT NEUTRINO TYPES FROM COLLIDER EXPERIMENTS

Revised August 2001 by D. Karlen (Carleton University).

The most precise measurements of the number of light neutrino types,  $N_\nu$ , come from studies of  $Z$  production in  $e^+e^-$  collisions. The invisible partial width,  $\Gamma_{\text{inv}}$ , is determined by subtracting the measured visible partial widths, corresponding to  $Z$  decays into quarks and charged leptons, from the total  $Z$  width. The invisible width is assumed to be due to  $N_\nu$  light neutrino species each contributing the neutrino partial width  $\Gamma_\nu$  as given by the Standard Model. In order to reduce the model dependence, the Standard Model value for the ratio of the neutrino to charged leptonic partial widths,  $(\Gamma_\nu/\Gamma_\ell)_{\text{SM}} = 1.991 \pm 0.001$ , is used instead of  $(\Gamma_\nu)_{\text{SM}}$  to determine the number of light neutrino types:

$$N_\nu = \frac{\Gamma_{\text{inv}}}{\Gamma_\ell} \left( \frac{\Gamma_\ell}{\Gamma_\nu} \right)_{\text{SM}} . \quad (1)$$

The combined result from the four LEP experiments is  $N_\nu = 2.984 \pm 0.008$  [1].

In the past, when only small samples of  $Z$  decays had been recorded by the LEP experiments and by the Mark II at SLC, the uncertainty in  $N_\nu$  was reduced by using Standard Model fits to the measured hadronic cross sections at several center-of-mass energies near the  $Z$  resonance. Since this method is much more dependent on the Standard Model, the approach described above is favored.

Before the advent of the SLC and LEP, limits on the number of neutrino generations were placed by experiments at lower-energy  $e^+e^-$  colliders by measuring the cross section of the process  $e^+e^- \rightarrow \nu\bar{\nu}\gamma$ . The ASP, CELLO, MAC, MARK J, and VENUS experiments observed a total of 3.9 events above background [2], leading to a 95% CL limit of  $N_\nu < 4.8$ . This process has a much larger cross section at center-of-mass energies near the  $Z$  mass and has been measured at LEP by the ALEPH, DELPHI, L3, and OPAL experiments [3]. These experiments have observed several thousand such events, and the combined result is  $N_\nu = 3.00 \pm 0.08$ . The same process has also been measured by the LEP experiments at much higher center-of-mass energies, between 130 and 208 GeV, in searches for new physics [4]. Combined, the measured cross section is  $0.982 \pm 0.012$  (stat) of that expected for three light neutrino generations [5].

Experiments at  $p\bar{p}$  colliders also placed limits on  $N_\nu$  by determining the total  $Z$  width from the observed ratio of  $W^\pm \rightarrow \ell^\pm\nu$  to  $Z \rightarrow \ell^+\ell^-$  events [6]. This involved a calculation that assumed Standard Model values for the total  $W$  width and the ratio of  $W$  and  $Z$  leptonic partial widths, and used an estimate of the ratio of  $Z$  to  $W$  production cross sections. Now that the  $Z$  width is very precisely known from the LEP experiments, the approach is now one of those used to determine the  $W$  width.

## References

1. The LEP Collaborations and the LEP Electroweak Working Group, as reported by J. Dress at the *XX International Symposium on Lepton and Photon Interactions at High Energy*, Rome, Italy (July 2001).

2. VENUS: K. Abe *et al.*, Phys. Lett. **B232**, 431 (1989);  
ASP: C. Hearty *et al.*, Phys. Rev. **D39**, 3207 (1989);  
CELLO: H.J. Behrend *et al.*, Phys. Lett. **B215**, 186 (1988);  
MAC: W.T. Ford *et al.*, Phys. Rev. **D33**, 3472 (1986);  
MARK J: H. Wu, Ph.D. Thesis, Univ. Hamburg (1986).
3. L3: M. Acciarri *et al.*, Phys. Lett. **B431**, 199 (1998);  
DELPHI: P. Abreu *et al.*, Z. Phys. **C74**, 577 (1997);  
OPAL: R. Akers *et al.*, Z. Phys. **C65**, 47 (1995);  
ALEPH: D. Buskulic *et al.*, Phys. Lett. **B313**, 520 (1993).
4. OPAL: G. Abbiendi *et al.*, Eur. Phys. J. **C18**, 253 (2000);  
DELPHI: P. Abreu *et al.*, Eur. Phys. J. **C17**, 53 (2000);  
L3: M. Acciarri *et al.*, Phys. Lett. **B470**, 268 (1999);  
ALEPH: R. Barate *et al.*, Phys. Lett. **B429**, 201 (1998).
5. The LEP Collaborations and the LEP SUSY Working Group, LEPSUSYWG/01-05.1.
6. UA1: C. Albajar *et al.*, Phys. Lett. **B198**, 271 (1987);  
UA2: R. Ansari *et al.*, Phys. Lett. **B186**, 440 (1987).

### Number from $e^+e^-$ Colliders

#### Number of Light $\nu$ Types

Our evaluation uses the invisible and leptonic widths of the Z boson from our combined fit shown in the Particle Listings for the Z Boson, and the Standard Model value  $\Gamma_\nu/\Gamma_\ell = 1.9908 \pm 0.0015$ .

VALUE	DOCUMENT ID	TECN
<b>2.994±0.012 OUR EVALUATION</b>	Combined fit to all LEP data.	

• • • We do not use the following data for averages, fits, limits, etc. • • •

3.00 ± 0.05	<sup>1</sup> LEP	92 RVUE
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<sup>1</sup> Simultaneous fits to all measured cross section data from all four LEP experiments.

#### Number of Light $\nu$ Types from Direct Measurement of Invisible Z Width

In the following, the invisible Z width is obtained from studies of single-photon events from the reaction  $e^+e^- \rightarrow \nu\bar{\nu}\gamma$ . All are obtained from LEP runs in the  $E_{\text{cm}}^{ee}$  range 88–209 GeV.

VALUE	DOCUMENT ID	TECN	COMMENT
<b>2.93±0.05 OUR AVERAGE</b>	Error includes scale factor of 1.2.		
2.98±0.05±0.04	ACHARD	04E L3	1990-2000 LEP runs
2.86 ± 0.09	HEISTER	03C ALEP	$\sqrt{s}=189-209$ GeV
2.69±0.13±0.11	ABBIENDI,G	00D OPAL	1998 LEP run
2.84±0.15±0.14	ABREU	00Z DLPH	1997-1998 LEP runs
2.89±0.32±0.19	ABREU	97J DLPH	1993-1994 LEP runs
3.23±0.16±0.10	AKERS	95C OPAL	1990-1992 LEP runs
2.68±0.20±0.20	BUSKULIC	93L ALEP	1990-1991 LEP runs

• • • We do not use the following data for averages, fits, limits, etc. • • •

3.01±0.08 ACCIARRI 99R L3 1991–1998 LEP runs  
 3.1 ±0.6 ±0.1 ADAM 96C DLPH  $\sqrt{s} = 130, 136$  GeV

## Limits from Astrophysics and Cosmology

### Number of Light $\nu$ Types

(“light” means  $<$  about 1 MeV). See also OLIVE 81. For a review of limits based on Nucleosynthesis, Supernovae, and also on terrestrial experiments, see DENEGRI 90. Also see “Big-Bang Nucleosynthesis” in this Review.

<u>VALUE</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
$< 4.4$	<sup>2</sup> CYBURT	05	COSM
$< 3.3$	<sup>3</sup> BARGER	03C	COSM
$1.4 < N_\nu < 6.8$	<sup>4</sup> CROTTY	03	COSM
$1.9 < N_\nu < 7.0$	<sup>5</sup> HANNESTAD	03B	COSM
$1.9 < N_\nu < 6.6$	<sup>4</sup> PIERPAOLI	03	COSM
$2 < N_\nu < 4$	LISI	99	BBN
$< 4.3$	OLIVE	99	BBN
$< 4.9$	COPI	97	Cosmology
$< 3.6$	HATA	97B	High D/H quasar abs.
$< 4.0$	OLIVE	97	BBN; high $^4\text{He}$ and $^7\text{Li}$
$< 4.7$	CARDALL	96B	Cosmology, High D/H quasar abs.
$< 3.9$	FIELDS	96	Cosmology, BBN; high $^4\text{He}$ and $^7\text{Li}$
$< 4.5$	KERNAN	96	Cosmology, High D/H quasar abs.
$< 3.6$	OLIVE	95	BBN; $\geq 3$ massless $\nu$
$< 3.3$	WALKER	91	Cosmology
$< 3.4$	OLIVE	90	Cosmology
$< 4$	YANG	84	Cosmology
$< 4$	YANG	79	Cosmology
$< 7$	STEIGMAN	77	Cosmology
	PEEBLES	71	Cosmology
$< 16$	<sup>6</sup> SHVARTSMAN	69	Cosmology
	HOYLE	64	Cosmology

<sup>2</sup> Limit on the number of neutrino types based on  $^4\text{He}$  and D/H abundance assuming a baryon density fixed to the WMAP data. Limit relaxes to 4.6 if D/H is not used or to 5.8 if only D/H and the CMB are used. See also CYBURT 01 and CYBURT 03.

<sup>3</sup> Limit on the number of neutrino types based on combination of WMAP data and big-bang nucleosynthesis. The limit from WMAP data alone is 8.3. See also KNELLER 01.  $N_\nu \geq 3$  is assumed to compute the limit.

<sup>4</sup> 95% confidence level range on the number of neutrino flavors from WMAP data combined with other CMB measurements, the 2dfGRS data, and HST data.

<sup>5</sup> 95% confidence level range on the number of neutrino flavors from WMAP data combined with other CMB measurements, the 2dfGRS data, HST data, and SN1a data.

<sup>6</sup> SHVARTSMAN 69 limit inferred from his equations.

### Number Coupling with Less Than Full Weak Strength

<u>VALUE</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●		
$< 20$	<sup>7</sup> OLIVE	81C COSM
$< 20$	<sup>7</sup> STEIGMAN	79 COSM

<sup>7</sup> Limit varies with strength of coupling. See also WALKER 91.

## REFERENCES FOR Limits on Number of Neutrino Types

CYBURT	05	ASP 23 313	R.H. Cyburt <i>et al.</i>	
ACHARD	04E	PL B587 16	P. Achard <i>et al.</i>	(L3)
BARGER	03C	PL B566 8	V. Barger <i>et al.</i>	
CROTTY	03	PR D67 123005	P. Crotty, J. Lesgourgues, S. Pastor	
CYBURT	03	PL B567 227	R.H. Cyburt, B.D. Fields, K.A. Olive	
HANNESTAD	03B	JCAP 0305 004	S. Hannestad	
HEISTER	03C	EPJ C28 1	A. Heister <i>et al.</i>	(ALEPH Collab.)
PIERPAOLI	03	MNRAS 342 L63	E. Pierpaoli	
CYBURT	01	ASP 17 87	R.H. Cyburt, B.D. Fields, K.A. Olive	
KNELLER	01	PR D64 123506	J.P. Kneller <i>et al.</i>	
ABBIENDI,G	00D	EPJ C18 253	G. Abbiendi <i>et al.</i>	(OPAL Collab.)
ABREU	00Z	EPJ C17 53	P. Abreu <i>et al.</i>	(DELPHI Collab.)
ACCIARRI	99R	PL B470 268	M. Acciarri <i>et al.</i>	(L3 Collab.)
LISI	99	PR D59 123520	E. Lisi, S. Sarkar, F.L. Villante	
OLIVE	99	ASP 11 403	K.A. Olive, D. Thomas	
ABREU	97J	ZPHY C74 577	P. Abreu <i>et al.</i>	(DELPHI Collab.)
COPI	97	PR D55 3389	C.J. Copi, D.N. Schramm, M.S. Turner	(CHIC)
HATA	97B	PR D55 540	N. Hata <i>et al.</i>	(OSU, PENN)
OLIVE	97	ASP 7 27	K.A. Olive, D. Thomas	(MINN, FLOR)
ADAM	96C	PL B380 471	W. Adam <i>et al.</i>	(DELPHI Collab.)
CARDALL	96B	APJ 472 435	C.Y. Cardall, G.M. Fuller	(UCSD)
FIELDS	96	New Ast 1 77	B.D. Fields <i>et al.</i>	(NDAM, CERN, MINN+)
KERNAN	96	PR D54 3681	P.S. Kernan, S. Sarkar	(CASE, OXFTP)
AKERS	95C	ZPHY C65 47	R. Akers <i>et al.</i>	(OPAL Collab.)
OLIVE	95	PL B354 357	K.A. Olive, G. Steigman	(MINN, OSU)
BUSKULIC	93L	PL B313 520	D. Buskulic <i>et al.</i>	(ALEPH Collab.)
LEP	92	PL B276 247	LEP Collabs.	(LEP, ALEPH, DELPHI, L3, OPAL)
WALKER	91	APJ 376 51	T.P. Walker <i>et al.</i>	(HSCA, OSU, CHIC+)
DENEGRI	90	RMP 62 1	D. Denegri, B. Sadoulet, M. Spiro	(CERN, UCB+)
OLIVE	90	PL B236 454	K.A. Olive <i>et al.</i>	(MINN, CHIC, OSU+)
YANG	84	APJ 281 493	J. Yang <i>et al.</i>	(CHIC, BART)
OLIVE	81	APJ 246 557	K.A. Olive <i>et al.</i>	(CHIC, BART)
OLIVE	81C	NP B180 497	K.A. Olive, D.N. Schramm, G. Steigman	(EFI+)
STEIGMAN	79	PRL 43 239	G. Steigman, K.A. Olive, D.N. Schramm	(BART+)
YANG	79	APJ 227 697	J. Yang <i>et al.</i>	(CHIC, YALE, VIRG)
STEIGMAN	77	PL 66B 202	G. Steigman, D.N. Schramm, J.E. Gunn	(YALE, CHIC+)
PEEBLES	71	Physical Cosmology	P.Z. Peebles	(PRIN)
		Princeton Univ. Press (1971)		
SHVARTSMAN	69	JETPL 9 184	V.F. Shvartsman	(MOSU)
		Translated from ZETFP 9 315.		
HOYLE	64	NAT 203 1108	F. Hoyle, R.J. Tayler	(CAMB)